

Math 303, Worksheet #3
Fall 2008

Name: _____

Use these vectors in each of the problems below.

$$\vec{v}_1 = 3\vec{i} - 2\vec{j}$$

$$\vec{v}_2 = \vec{i} + \vec{j}$$

$$\vec{v}_3 = 4\vec{i} + 3\vec{j}$$

$$\vec{v}_4 = 3\vec{i} - 2\vec{j} + \vec{k}$$

$$\vec{v}_5 = -2\vec{i} + \vec{j} + 3\vec{k}$$

$$\vec{v}_6 = \vec{i} + \vec{j} + \vec{k}$$

1. Compute each of the following:

a. $\vec{v}_1 \cdot \vec{v}_2$

b. $3(\vec{v}_3 \cdot \vec{v}_4)(\vec{v}_5 \cdot \vec{v}_6)$

c. $(\vec{v}_4 \cdot \vec{v}_5)\vec{v}_6$

d. $\vec{v}_4(\vec{v}_5 \cdot \vec{v}_6)$

2. The Maple command for the dot product is DotProduct, so to compute $v \cdot w$ type:

restart:with(LinearAlgebra):

DotProduct(v,w)

a.

Use Maple to check each of your answers above.

3. Find a nonzero vector which is orthogonal to \vec{v}_2 . There is more than one correct answer.

4. Find a nonzero vector which is orthogonal to \vec{v}_4 . There is more than one correct answer.

5. Find the angle between \vec{v}_4 and \vec{v}_5

There is another vector product of vectors \vec{v} and \vec{w} , called the cross product, written $\vec{v} \times \vec{w}$. The Maple command for the cross product is (not surprisingly) `CrossProduct`. So to compute $v \times w$ type:

`CrossProduct(v,w)`

6. Compute each of the following

a. $(\vec{i} + \vec{j} + \vec{k}) \times (\vec{i} - \vec{j})$

b. $(\vec{i} - \vec{j}) \times (\vec{i} + \vec{j} + \vec{k})$

c. $\vec{i} \times \vec{j}$

d. $\vec{j} \times \vec{k}$

e. $\vec{k} \times \vec{i}$

f. $(a\vec{i} + b\vec{j} + c\vec{k}) \times (d\vec{i} + e\vec{j} + f\vec{k})$